

# Chapter 18

## Electric Currents

# Current

- = motion of charge

a steady flow of charge → a steady force on mobile charges

$$I = \frac{\Delta Q}{\Delta t}$$

current = amount  
of charge moving  
through given  
cross section per  
unit time

[I] = ampere, 1 A = 1 C / s


# Current in a Complete Circuit

- current is the same at all cross sections, it does not emerge from the positive battery terminal and disappear in the negative terminal
- speed to establish current  $\gg$  electron drift speed

conventional current flow:  
from + to – (opposite to  
electron motion)

# Resistance and Resistivity

Electric field is proportional to the potential difference between the ends of a conductor, and current is caused by electric field

$$R = \frac{V}{I}$$


**Ohm's law:** For many materials, current is proportional to potential difference (voltage)

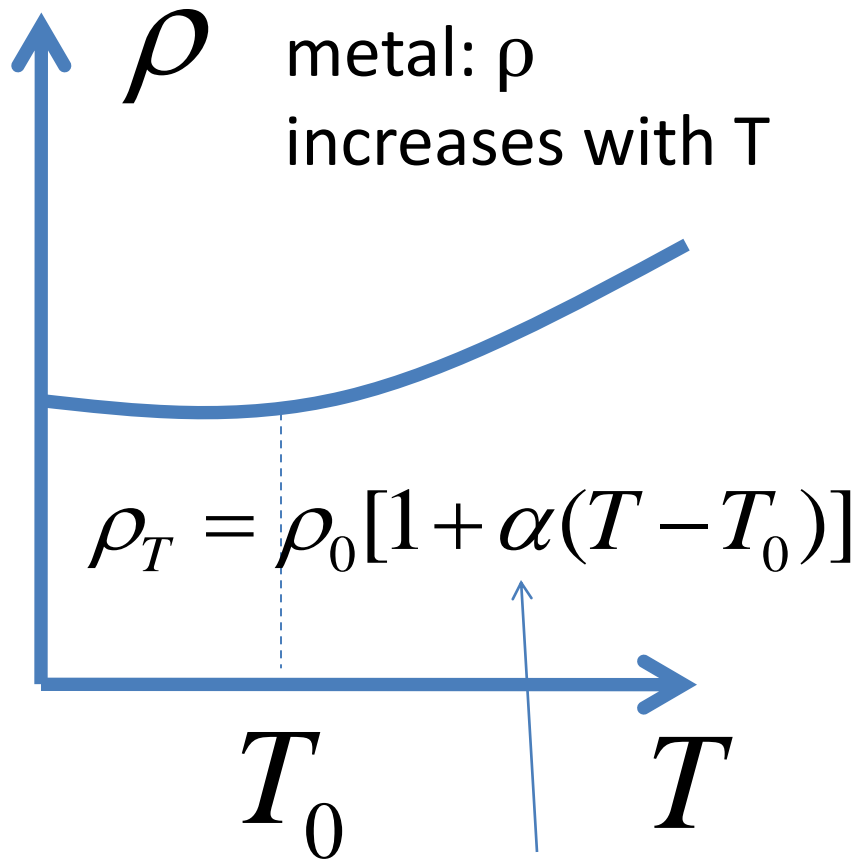
**Resistance:** the proportionality factor

Resistance is for an object,  
resistivity for material

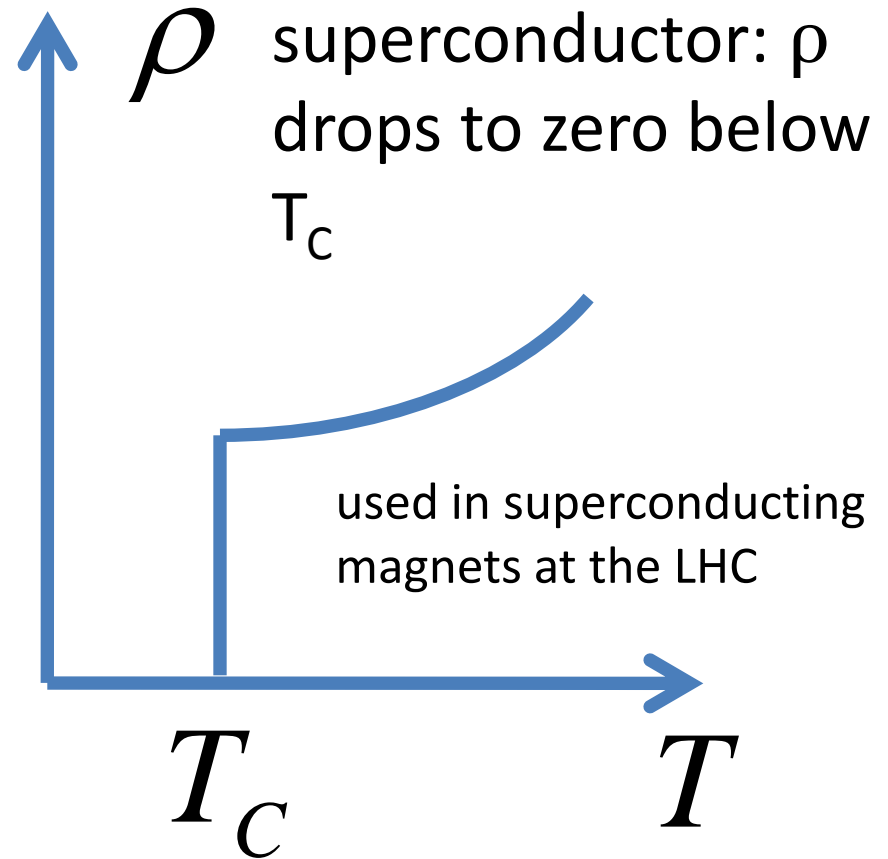
**Resistivity  $\rho$ :**  
geometry  
independent

$$R = \rho \frac{L}{A}$$

# Temperature Dependence of R



temperature coefficient of resistivity



# Energy and Power in Circuits

- as charge passes through a circuit, the electric field does work on the charge

$$\Delta W = V\Delta Q \leftarrow \text{definition of potential difference}$$

$$\Delta Q = I\Delta t \leftarrow \text{definition of current}$$

$$VI = \frac{\Delta W}{\Delta t} = P$$

power = work/unit time

from Ohm's law:

$$P = I^2 R = \frac{V^2}{R}$$

# Alternating Current

- Direct current: charges move steadily in one direction
- Alternating current: the direction changes over time

$$V = V_0 \sin \omega t$$

$$I = \frac{V}{R} = \frac{V_0}{R} \sin \omega t = I_0 \sin \omega t$$

# Alternating Current Power

- Power is always positive, can talk about average power

$$P = I^2 R = I_0^2 \sin^2 \omega t$$
$$I_{\text{rms}} = I_0 / \sqrt{2}$$
$$\bar{P} = \frac{1}{2} I_0^2 R = \frac{1}{2} \frac{V_0^2}{R}$$
$$V_{\text{rms}} = V_0 / \sqrt{2}$$
$$\bar{P} = I_{\text{rms}} V_{\text{rms}}$$