

### Formula sheet for Final PHYS 3113

First law of thermodynamics:  $\Delta U = Q + W$ ,  $W = -\int PdV$

Thermodynamic identity:  $dU = TdS - PdV$

Ideal gas:  $PV = NkT$ ,  $U = \frac{f}{2}NkT$

Heat capacity:  $C = \frac{\partial U}{\partial T}$

Boltzmann statistics:  $Z = \sum e^{-\beta E_n}$ ,  $\beta = \frac{1}{kT}$      $\langle E \rangle = -\frac{1}{Z} \frac{\partial Z}{\partial \beta}$      $U = N\langle E \rangle$

Fermi gas of electrons in solids:  $\epsilon_F = \frac{\hbar^2}{8m} \left( \frac{3N}{\pi V} \right)^{2/3}$

internal energy at low  $T$ :  $U = \frac{3}{5}N\epsilon_F + \frac{\pi^2}{4}N \frac{(kT)^2}{\epsilon_F}$

Debye theory of solids (lattice vibrations):  $T_D = \frac{\hbar c_S}{2k} \left( \frac{6N}{\pi V} \right)^{1/3}$

internal energy at low  $T$ :  $U = \frac{3\pi^4}{5} \frac{NkT^4}{T_D^3}$

Bose-Einstein condensation:  $T_c = \gamma \frac{\hbar^2}{2\pi m k} \left( \frac{N}{V} \right)^{2/3}$ ,  $\gamma = 0.527$

$N_0 = N - N_{\text{excited}} = \left[ 1 - \left( \frac{T}{T_c} \right)^{3/2} \right] N$

Useful constants:

$k = 1.38 \times 10^{-23} \text{ J/K}$      $1 \text{ eV} = 1.602 \times 10^{-19} \text{ J}$      $kT = 0.026 \text{ eV} \left( \frac{T}{300 \text{ K}} \right)$